Detection of GNSS Signals Propagation in Urban Canyons Using 3D City Models

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Abstract. This paper presents one of the solutions to the problem of multipath propagation and effects on Global Navigation Satellite Systems (GNSS) signals in urban canyons. GNSS signals may reach a receiver not only through Line-of-Sight (LOS) paths, but they are often blocked, reflected or diffracted from tall buildings, leading to unmodelled GNSS errors in position estimation. Therefore in order to detect and mitigate the impact of multipath, a new ray-tracing model for simulation of GNSS signals reception in urban canyons is proposed - based on digital 3D maps information, known positions of GNSS satellites and an assumed position of a receiver. The model is established and validated using experimental, as well as real data. It is specially designed for complex environments and situations where positioning with highest accuracy is required - a typical example is navigation for blind people.

Keywords

3D buildings models, blind navigation, GNSS signal propagation, LOS, multipath, path delay estimation, urban canyons.

1. Introduction

The aim of this paper is to describe the calculation of GNSS signal parameters in a complex environment with multiple reflections taking the knowledge of the receiver position in account. This approach can be used to estimate the subject’s unknown position while moving in the same environment.

It is well known that multipath is a phenomenon that represents a dominant error source in precise GNSS positioning. In dynamic urban environment, it changes rapidly and therefore it is difficult to detect, predict or control.

Generally, the direct (or Line-of-Sight, LOS) signal is normally the most wanted signal. Nevertheless signals can also arrive at a receiver via a number of different paths that may occur between a satellite and a receiver. These paths are results of reflections and diffractions from buildings, water, ground etc.

Typically, an antenna receives the direct signal and one or more of its reflections. A reflected signal is usually a weaker version of the direct signal and takes more time to reach the receiver than the direct signal. This path delay, or better this difference between length of the path taken by the reflected signal and the direct signal between a satellite and a receiver, causes an important pseudorange measurement error [1], [2] and [3], as shown in Fig. 1 and Fig. 2. Reception of reflected signals also causes distortion in the code correlation peak within the receiver therefore the code phase of the direct LOS signal cannot be precisely determined.

Fig. 1: The real path of the user in urban canyon.
Different multipath mitigation techniques were developed to improve positioning performance in built up areas. One promising solution is to use multiple satellite constellations with combination of 3D building models to calculate the path length of direct signals or better path delay of reflected signals and thus to eliminate multipath impact on GNSS signals.

There are several satellite systems in operation today - the US NAVSTAR Global Positioning System (GPS), or the Russian GLONASS (Global’na Navigatsionnaya Sputnikovaya Sistema). Chinese Compass navigation system and the European Union’s Galileo navigation system are currently under construction.

2. Background

In order to understand multipath effects it is necessary to understand the electromagnetic wave properties and changes a GNSS signal goes through on the path from a satellite to a receiver. How the position is computed using pseudoranges and the typical multipath error in pseudorange measurements is also explained in this section.

2.1. Electromagnetic Wave Properties

A GNSS signal is a Right-Hand Circularly Polarized (RHCP) transverse electromagnetic wave - it means a wave where the electric and magnetic fields oscillate perpendicularly to and in phase with one another, and is perpendicular to the direction of propagation [1], [2] and [4].

Mathematical representation of a plane wave propagating in the direction $x$ can be written as [5]:

$$\vec{E} = \vec{E}_0 \cos(kx - \omega t + \varphi_0),$$

where $\vec{E}_0$ is the amplitude, $k$ is the propagation constant, $\omega$ is the circular frequency and $\varphi_0$ is the phase constant:

$$k = \frac{2\pi}{\lambda},$$

$$\omega = kc = \frac{2\pi c}{\lambda},$$

$$\varphi = (kx - \omega + \varphi_0),$$

and $\varphi$ is the phase of the plane wave.

The electric field vector $\vec{E}$ may be decomposed into the parallel $E_l$ and perpendicular $E_r$ components as:

$$E_l = E_{l0} \cos(kx - \omega t + \varphi_{l0}),$$

$$E_r = E_{r0} \cos(kx - \omega t + \varphi_{r0}),$$

with a simple manipulation we get:

$$\frac{E_l}{E_{l0}} = \cos(v) \cos(\varphi_{l0}) - \sin(v) \sin(\varphi_{l0}),$$

$$\frac{E_r}{E_{r0}} = \cos(v) \cos(\varphi_{r0}) - \sin(v) \sin(\varphi_{r0}),$$

where:

$$v = kx - \omega t,$$

then we obtain:

$$\left(\frac{E_l}{E_{l0}}\right)^2 + \left(\frac{E_r}{E_{r0}}\right)^2 - \frac{E_l}{E_{l0}} \cdot \frac{E_r}{E_{r0}} \cos(\Delta \varphi) = \sin^2(\Delta \varphi),$$

when $\Delta \varphi = n\pi/2 \ (n = \pm 1, \pm 3, \ldots)$, $E_{l0} = E_{r0} = E_0$, $\sin(\Delta \varphi) = \pm 1$ and $\cos(\Delta \varphi) = 0$ then Eq. (10) becomes:

$$E_l^2 + E_r^2 = E_0^2,$$

and Eq. (11) defines a circle or circularly polarized wave.

Electromagnetic waves don’t propagate in straight lines (expect in a vacuum where they travel at $3 \cdot 10^8$ m·s$^{-1}$), they are bent as they pass through the different layers of the earth’s atmosphere to the earth - this increases the GNSS signal travel time from the satellite to the receiver [4].
2.2. Propagation of GNSS Signals in Urban Environment

The propagation of GNSS signals is mainly impacted of three possible examples - reflection, diffraction and refraction \[4\], as illustrated in Fig. 3.

For our research we expect the GNSS signal to be a straight line. Therefore the proposed algorithm considers reflection and diffraction examples only.

Reflection is a process where a wave enters a different medium and its parameters can change at the boundary of the two media (i.e. speed, wavelength, and energy). The Law of Reflection states that the angle of incidence equals to the angle of reflection. Furthermore, the incident ray, the normal to the surface, and the reflected ray all lie in the same plane. As a special case is considered scattering - a wave reflects at all angles (i.e. reflection that doesn’t obey the Law of Reflection).

Diffraction is bending of a wave process as it travels past the edge of or around sharps corners (for more look at Huygens’ principle of wave diffraction) \[4\].

2.3. Position Computation

The position is computed from pseudoranges and satellite positions \((X^k, Y^k, Z^k)\) found from ephemerides data. The most commonly used algorithm for position computations from pseudoranges is based on the method of least-squares. This method is used when there are more observations than unknowns. A pseudorange is the time the signal travelled from the satellite to the receiver, multiplied by the speed of light \[6\],

\[d_{orange} = \text{time the signal travelled from the satellite to the receiver} \times \text{speed of light} \]

There are more observations than unknowns. A pseudorange is the time the signal travelled from the satellite to the receiver, multiplied by the speed of light \[6\], therefore to compute the position at least four pseudoranges are needed. Before using the least-squares method, Eq. \((13)\) has to be linearized.

Let \(c\) denote the speed of light, \(dt_i\) be the receiver clock offset, \(dt^k\) be the satellite clock offset, be the tropospheric delay, be the ionospheric delay and be the observational error of the pseudorange. Then the basic equation for the pseudorange \(P_i^k\):

\[P_i^k = p_i^k + c(\text{dt}_i - \text{dt}^k) + T_i^k + I_i^k + e_i^k. \quad (13)\]

The position of the satellite \((X^k, Y^k, Z^k)\) and satellite clock offset \(dt^k\) are found in the ephemerides, the tropospheric delay and the ionospheric delay \(T_i^k\) and the ionospheric delay \(I_i^k\) are computed from different a priori models, the error \(e_i^k\) is minimized by using the least-squares method.

2.4. Multipath Error in Pseudorange

Typical multipath error in pseudorange measurements differs from 1 m (in a fair environment) to more than 5 m (in highly reflective environment) and the phase measurement error doesn’t exceed a quarter cycles (if the reflected signal has smaller amplitude than the direct signal), \[11\]:

Consider an antenna receives two signals: a direct signal and a delayed reflected signal with phase shift \(\Delta \phi\) and amplitude attenuation \(\alpha\).

\[
\text{received_signal} = A \cos \phi + \alpha A \cos (\phi + \Delta \phi). \quad (14)
\]

The error in the carrier phase measurement due to the multipath is as:

\[
\delta \phi = \arctan \left( \frac{\sin \Delta \phi}{\alpha^{-1} + \cos \Delta \phi} \right), \quad (15)
\]

in the worst case \(\delta \phi = 90^\circ\), for \(\alpha > 1\).

3. Urban Modelling Methodology

In this section, the urban modelling methodology for creating a 3D model is introduced. At first, we describe how to extract building geometry of a given environment with coordinate data into a file to be able to read data in Matlab. Afterwards, the known coordinates of satellites are obtained from navigation messages. Finally, a conversion between the satellite coordinate system into the mapping coordinate system used for our calculations is presented.
3.1. 3D Environment Modelling

1) 3D Geometry Extraction

To capture and extract 3D building geometry with textures and coordinate data from Google Earth into a .3dr file, 3D Ripper DX was used. The conversion to .obj file was done in Autodesk 3ds Max 2011, and then changed in Mathematica to .csv file.

2) 3D Environment for Plotting and Calculations

The environment was simulated in Matlab using .csv geometry coordinates data, considering the building layout to be made up of triangles (vertices A, B, C) put together.

3.2. Satellite Coordinates

The known positions of satellites are calculated from ephemeris data and are found in the navigation message, i.e. in [9].

1) Conversion of Satellite Coordinates into Mapping Coordinates

The obtained satellites coordinates in earth-centred earth-fixed (ECEF) WGS-84 system \((X_s, Y_s, Z_s)\) are transformed into the mapping coordinates \((X_m, Y_m, Z_m)\) using the following matrix \(M_{ECEF\_MC}\):

\[
M_{ECEF\_MC} = \begin{pmatrix}
-\sin(\beta) & \cos(\beta) & 0 \\
-\cos(\beta) \cdot \sin(\alpha) & -\sin(\beta) \cdot \sin(\alpha) & \cos(\alpha) \\
\cos(\alpha) \cdot \cos(\beta) & \cos(\beta) \cdot \sin(\alpha) & \sin(\alpha)
\end{pmatrix},
\]

(16)

where \(\alpha\) and \(\beta\) represent latitude (N) and longitude (E) coordinates converted to radians.

4. Mathematical Model

In the following, the proposed multipath detection model for dynamic propagation environments is presented. To investigate whether GNSS signals arrived at a receiver directly or through reflections, the ray-tracing algorithm is introduced based on information obtained from 3D buildings model, assumed position of the receiver and known positions of GNSS satellites extracted from navigation message. In section 4.1, calculation of direct path between a satellite and a receiver is described. In section 4.2, possible reflections of a GNSS signal are calculated, the coordinates of reflection points are determined and thus the reflection length (or the signal path delay) is computed.

4.1. Calculation of Direct Path

Consider a ray (vector \(\overrightarrow{SP}\)) from \(S\) (satellite) to \(P\) (receiver), and a triangle with vertices \(A, B, C\) (obtained from the 3D map), as shown in Fig. 4. To avoid all points \((S, P, A, B, C)\) to be on one line, the algorithm provides an estimate of the number of linearly independent vectors \(\overrightarrow{AB}, \overrightarrow{AC},\) and \(\overrightarrow{SP}\).

To get the intersection of the vector \(\overrightarrow{SP}\) with the \(\Delta ABC\), we first determine the intersection of the vector \(\overrightarrow{SP}\) and a plane \((\Delta ABC \in \rho)\) as mentioned in section 3.1. If it does not intersect, then it also does not intersect the \(\Delta ABC\) and the time and distance from a given satellite to the receiver are calculated from pseudoranges, as in Eq. (12). However, if they intersect in the point \(R\) (reflection), we need to determine if this point is inside the \(\Delta ABC\). A limitation is done to exclude the intersection point \(R\) as a part of the ray \(\overrightarrow{SP}\) \((R \notin \overrightarrow{SP})\).

Fig. 4: Illustration of GNSS signal - direct path.

1) Intersection of a Ray with a Plane

A plane is defined by three non-collinear points (three points not on a line) \(A, B, C\). These three points define two distinct vectors \(\overrightarrow{AB}\) and \(\overrightarrow{AC}\). The \(\Delta ABC\) lies in the plane \(\rho\) through \(A\) with normal vector \(\vec{n}\) [1], [10]:

\[
\vec{n} = \overrightarrow{AB} \times \overrightarrow{AC}.
\]

(17)

Then the parametric plane equation through a point is:

\[
R = A + (\overrightarrow{BA}) \cdot s + (\overrightarrow{CA}) \cdot u,
\]

(18)

where \(s, u \in \mathbb{R}\).
The parametric equation of a ray that passes through a point is:

\[ R = P + \left( \frac{PS}{d} \right) \cdot t, \]

where \( t \in \mathbb{R} \).

By inserting Eq. (19) to Eq. (18), we get the solution to \( t, s, u \):

\[
\mathbf{M}_{t,s,u} = \\
\begin{pmatrix}
S_x - P_x & B_x - A_x & C_x - A_x & P_x - A_x \\
S_y - P_y & B_y - A_y & C_y - A_y & P_y - A_y \\
S_z - P_z & B_z - A_z & C_z - A_z & P_z - A_z
\end{pmatrix}.
\]

By substituting the solution of Eq. (20) into Eq. (18), we get the solution to \( R \) in the plane.

4.2. Calculation of Multipath Reflections

1) Single Reflection - Calculation of Reflection Length

Areas with buildings on one side are considered for this model, as shown in Fig. 5. The basic criteria to determine whether a point lies in a triangle or on the edge of a triangle are as \([4], [9]\):

\[
\alpha_1 + \alpha_2 + \alpha_3 \leq 1,
\]

\[
\alpha_1, \alpha_2, \alpha_3 \geq 1,
\]

where \( \alpha_1, \alpha_2, \alpha_3 \in \mathbb{R} \).

By substituting the solution of \( t \) in the parametric coordinates of the intersection point \( R \) in the plane.

To determine whether the intersection point \( R \) lies inside or on an edge of the \( \Delta ABC \), the algorithm verifies the conditions described in Eq. (21) and Eq. (22).

Given by known coordinates of \( S, R_1, \) and \( P \), the reflection length for a single reflection can be simply calculated as:

\[
delay = d_1 + d_2,
\]

where \( d_1 = |PR_1| \), and \( d_2 = |SR_1| \) in meters. From the knowledge that GNSS signals travel at the speed of light and the known distance to the receiver, we can simply calculate the time the signal took to reach the receiver.

The benefit of a single reflection is that after reflection the circular polarization of a GNSS signal is changed to left-handed (LHCP). An RHCP antenna can quite effective suppress the LHCP reflection and therefore minimize multipath reflection error. Naturally, a second reflection will cause the RHCP polarization again \([11], [12], [13]\).

2) Multiple Reflections - Calculation of Reflection Length

The benefit of a single reflection is that after reflection the circular polarization of a GNSS signal is changed to left-handed (LHCP). An RHCP antenna can quite effective suppress the LHCP reflection and therefore minimize multipath reflection error. Naturally, a second reflection will cause the RHCP polarization again \([11], [12], [13]\).

GNSS availability in urban environment is seriously degraded by buildings blocking direct signals from more than one side, as in Fig. 5.

From the knowledge of the single reflection point coordinates \( (R_x, R_y, R_z) \), the matrix describing reflections is found.

As in Eq. (19), the reflection point \( R \) can be expressed by:

\[
S + \tilde{n}_1 \cdot t_1 = P + \tilde{n}_2 \cdot t_2,
\]

where \( t_1, t_2 \in \mathbb{R} \), \( \tilde{n}_1 \) is the directional vector of the line \( |SR| \), \( \tilde{n}_2 \) is the directional vector of the line \( |RP| \).

The relation between these two directional vectors is given by:

\[
\tilde{n}_2 = \tilde{n}_1 \times \mathbf{M}_{REF},
\]

where \( \mathbf{M}_{REF} \) is the matrix describing reflection.

Let a triangle be defined with vertices \( A_x, B_x, C_x, \) \((x \in \mathbb{R})\) and vector \( \tilde{w} \) to be a normal vector to this plane:

\[
\tilde{w} = \overrightarrow{AB} \times \overrightarrow{AC},
\]

then the matrix \( \mathbf{M}_{REF} \) can be expressed as:

\[
\mathbf{M}_{REF} = \\
-\text{inv} \begin{pmatrix}
\tilde{w} \\
\overrightarrow{AB} \\
\overrightarrow{AC}
\end{pmatrix} \cdot \\
\begin{pmatrix}
-1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{pmatrix} \cdot \\
\begin{pmatrix}
\tilde{w} \\
\overrightarrow{AB} \\
\overrightarrow{AC}
\end{pmatrix}.
\]
Now when we know the reflection matrix, we can simply calculate if a GNSS signal arrived at the receiver via more than one reflection. For the illustration in Fig. 6:

Fig. 6: Illustration of multiple reflections on planar reflectors.

Fig. 6, given by known coordinates of $S$, $R_1$, $R_2$, $R_3$ and $P$, the reflection length for multiple reflections can be simply calculated as:

$$l_{\text{delay}} = d_1 + d_2 + d_3 + d_4,$$

where $d_1$ is $|PR_3|$, $d_2$ is $|R_2R_3|$, $d_3$ is $|R_1R_2|$, $d_4$ is $|PR_4|$ in meters.

From the knowledge that GNSS signals travel at the speed of light and the known distance to the receiver, we can calculate the time the signal took to reach the receiver.

5. Experimental Results

In this section, the evaluation methodology and results are presented. GNSS availability, integrity and precision were evaluated over pedestrian routes using different combinations of GNSS constellations. Measurements were performed in Europe and Asia for GPS, GLONASS, Galileo and Beidou.

In this case, we consider a building block in city model of Prague with variable parameters for street width, street length and building block parameters and known position of the receiver ($50^\circ 06'10.0''$ N, $14^\circ 23'24.18''$ E). Figure 7 shows a street captured in Google Earth used for our measurements as an example, Fig. 8 shows user view of the same street.

Figure 9 shows the same street after 3D geometry extraction into .obj file.

After extracting the navigation message and converting the satellites coordinates into the mapping coordinates Eq. (16), the algorithm described above is applied.

From the well-known position of the GNSS receiver and positions of currently available GNSS satellites in the view, the algorithm determines whether there is an obstacle in direct signal path or not.

As a result, we get a list of all direct paths and possible reflection examples (with mapping coordinates of...
points of reflection) for each satellite and the receiver, as shown in Tab. 1 and Tab. 2

Tab. 1: Results shown for GPS, satellite Nr. 5.

<table>
<thead>
<tr>
<th>Satellite Nr. 5</th>
<th>Direct Path:</th>
<th>Number of signals with a single reflection:</th>
<th>Point of reflection - coordinates (X₀, Y₀, Z₀):</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>1</td>
<td>1.0 · 10⁻² · [-1.8066, -0.6410, -0.0499]</td>
</tr>
</tbody>
</table>

Tab. 2: Results shown for GPS, satellite Nr. 7.

<table>
<thead>
<tr>
<th>Satellite Nr. 7</th>
<th>Direct Path:</th>
<th>Number of signals with a single reflection:</th>
<th>Number of signals with two reflections:</th>
<th>Point of reflection - coordinates (X₁₁, Y₁₁, Z₁₁):</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>0</td>
<td>3</td>
<td>1.0 · 10⁻² · [-1.3131, -0.7414, -0.0099]</td>
</tr>
</tbody>
</table>

Based on known coordinates of points of reflection, the time and the total propagation path length from a given satellite to the receiver are computed using Eq. (24) and Eq. (29). Computation time is extensively increasing with the amount of 3D map information, satellites, and receivers.

It is obvious that these facts can be used to compute the subject’s unknown position in a complex environment in reverse order. This will be shown in the following article in the future.

The principle of one of the possible methods can be described as a sequence of following steps:

- Determine the number of satellites visible using a combination of intelligent maps and known position of the subject.
- Perform calculations to determine the position (respectively the position in a presumed region) if the number of satellites that are in direct line-of-sight is greater than or equal to three.
- Based on combination of intelligent maps data, their calculations (including terrain and buildings height) and measured GNSS data (with known positions of satellites obtained from navigation message) - i.e. the interval halving method can be used to iterate data in so many steps until an agreement between measured and calculated parameters is reached and thus the determination of the actual position (with sufficient accuracy) is achieved.

This method can be combined with other options - i.e. in the first approximation, using an antenna capable of receiving only phase undistorted GNSS signals [13], or cameras able to determine which part of the sky is uninterrupted by objects etc.

6. Conclusion

The presence of reflected and diffracted signals in urban environments seriously degrades GNSS positioning in terms of accuracy, integrity and precision. Different combinations of GNSS constellations promise considerable improvements with respect to GPS only. Although, the current situation allows using just GPS and GLONASS fully, in the near future additional satellites of Galileo and Compass will offer significantly improved GNSS performance and availability.

Within this paper, a new ray-tracing model for simulation of GNSS signals reception in urban canyons was designed. The proposed multipath detection algorithm is based on digital 3D maps information, known positions of GNSS satellites and an assumed position of a receiver.

For each satellite, the algorithm determines whether a signal arrived at a receiver through a direct path or through multipath reflections. Furthermore, the algorithm can estimate the number of multipath reflections and their coordinate data within the proposed simulation system. With this information, the distance a signal travelled to the receiver, as well the transit time, is calculated.

Based on the research results presented in this paper, detection of GNSS signals propagation in urban environments can significantly improve accuracy of the pedestrian positioning. In the future work, an investigation in the multi constellation GNSS area and right selection of direct/multipath signals with one or more reflections for position calculation using the method presented seems to be interesting. It is also expected the data will be sent to the cloud for faster computation.

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References


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